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Extremal problem on (2n, 2m-1)-system points on the rays.

For fix number  $n \in \mathbb{N}$  system points

$$A_{2n,2m-1} = \{a_{k,p} \in \mathbb{C} : k = \overline{1,2m}, \ p = \overline{1,2m-1} \},$$

we will called on the (2n, 2m - 1)-system points on the rays, if at all  $k = \overline{1, 2m}$ ,  $p = \overline{1, 2m - 1}$  the relations are executed:

(1) 
$$\begin{aligned} 0 &< |a_{k,1}| < \ldots < |a_{k,2m-1}| < \infty; \\ \arg a_{k,1} &= \arg a_{k,2} = \ldots = \arg a_{k,2m-1} =: \theta_k; \\ 0 &= \theta_1 < \theta_2 < \ldots < \theta_n < \theta_{n+1} := 2\pi. \end{aligned}$$

Let's consider system of angular domains:

$$P_k = \{ w \in \mathbb{C} : \theta_k < \arg w < \theta_{k+1} \}, \quad k = \overline{1, 2n}.$$

Let  $D, D \subset \overline{\mathbb{C}}$  – arbitrary open set and  $w = a \in D$ , then D(a) the define connected component D, the contain point a. For arbitrary (2n, 2m-1)-system points on the rays  $A_{2n,2m-1} = \{a_{k,p} \in \mathbb{C} : k = \overline{1,2n}, \ p = \overline{1,2m-1}\}$  and open set  $D, A_{2n,2m-1} \subset D$  the define  $D_k(a_{s,p})$  connected component set  $D(a_{s,p}) \cap \overline{P_k}$ , the contain point  $a_{s,p}, k = \overline{1,2n}, \ s = k, k+1, \ p = \overline{1,2m-1}, \ a_{n+1,p} := a_{1,p}$ .

The open set D,  $A_{2n,2m-1} \subset D$  satisfied condition meets the condition of unapplied in relation to the system of points (2n, 2m-1)-system points on the rays  $A_{2n,2m-1}$  if a condition is executed

(2) 
$$D_k(a_{k,s}) \bigcap D_k(a_{k+1,p}) = \varnothing,$$

 $k = \overline{1, 2n}, p, s = \overline{1, 2m - 1}$  on all corners  $\overline{P_k}$ .

The define r(B; a) inner radius domain  $B \subset \overline{\mathbb{C}}$  with respect to a point  $a \in B$ . Subject of studying of our work are the following problem.

**Problem.** Let  $n, m \in \mathbb{N}, n \geq 2, m \geq 2, \alpha \in \mathbb{R}_+$ . Maximum functional be found

$$I = \prod_{k=1}^{n} \prod_{p=1}^{m} r^{\alpha} (D, a_{2k-1, 2p-1}) \cdot \prod_{k=1}^{n} \prod_{p=1}^{m-1} r (D, a_{2k-1, 2p}) \times \prod_{k=1}^{n} \prod_{p=1}^{m-1} r^{\alpha} (D, a_{2k, 2p}) \cdot \prod_{k=1}^{n} \prod_{p=1}^{m} r (D, a_{2k, 2p-1}),$$

where  $A_{2n,2m-1}$  – arbitrary (2n,2m-1)-system points on the rays, satisfied condition (1), D – arbitrary open set, the satisfied condition (2),  $a_{k,p} \in D \subset \overline{\mathbb{C}}$ , and all extremal the describe  $(k = \overline{1,2n}, p = \overline{1,2m-1})$ .

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